## Semester-VI <br> B. Sc (Honours) in Physics



DSE 4: Experimental Techniques

## Lecture <br> on

Statistical analysis of data

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## Lecture- III

## Syllabus

Measurements
$\square$ Accuracy and precision and Significant figures.
$\square$ Error and uncertainty analysis.

$\square$ Gross error,


Statistical analysis of data $\square$ Arithmetic mean, $\square$ Deviation from mean, Average deviation, $\square$ Standard deviation,
$\square$ Curve fitting.
Guassian distribution.

## Statistical analysis of data

Statistical data analysis is a procedure of performing various statistical operations. It is a kind of quantitative research, which seeks to quantify the data, and typically, applies some form of statistical analysis. Quantitative data basically involves descriptive data, such as survey data and observational data.

Two main statistical methods are used in data analysis: descriptive statistics, which summarize data from a sample using indexes such as the mean or standard deviation, and inferential statistics, which draw conclusions from data that are subject to random variation (e.g., observational errors, sampling variation).

## Arithmetic mean/ Deviation from mean/ Average deviation/ Standard deviation

Arithmetic mean : The average of a set of numerical values, as calculated by adding them together and dividing by the number of terms in the set.

Documents has been collected from<br>http://ncert.nic.in/ncerts/l/keep215.pdf

## Chaperer 15

## STATISTICS

### 15.1 Overview

In earlier classes, you have studied measures of central tendency such as mean, mode, median of ungrouped and grouped data. In addition to these measures, we often need to calculate a second type of measure called a measure of dispersion which measures the variation in the observations about the middle value- mean or median etc.

This chapter is concerned with some important measures of dispersion such as mean deviation, variance, standard deviation etc., and finally analysis of frequency distributions.

### 15.1.1 Measures of dispersion

(a) RangeThe measure of dispersion which is easiest to understand and easiest to calculate is the range. Range is defined as:
Range $=$ Largest observation - Smallest observation
(b) Mean Deviation
(i) Mean deviation for ungrouped data:

For $n$ observation $x_{1}, x_{2}, \ldots, x_{n}$, the mean deviation about their mean $\bar{x}$ is given by

$$
\begin{equation*}
\operatorname{M.D}(\bar{x})=\frac{\left|x_{i}-\bar{x}\right|}{n} \tag{1}
\end{equation*}
$$

Mean deviation about their median M is given by

$$
\begin{equation*}
\operatorname{M.D}(\mathrm{M})=\frac{\left|x_{i}-\mathrm{M}\right|}{n} \tag{2}
\end{equation*}
$$

## (ii) Mean deviation for discrete frequency distribution

Let the given data consist of discrete observations $x_{1}, x_{2}, \ldots, x_{n}$ occurring with frequencies $f_{1}, f_{2}, \ldots, f_{n}$, respectively. In this case

$$
\begin{align*}
& \operatorname{M.D}(\bar{x})=\frac{f_{i}\left|x_{i}-\bar{x}\right|}{f_{i}}=\frac{f_{i}\left|x_{i}-\bar{x}\right|}{\mathrm{N}}  \tag{3}\\
& \operatorname{M.D}(\mathrm{M})=\frac{f_{i}\left|x_{i}-\mathrm{M}\right|}{\mathrm{N}} \tag{4}
\end{align*}
$$

where $\mathrm{N}=f_{i}$.
(iii) Mean deviation for continuous frequency distribution (Grouped data).

$$
\begin{align*}
& \operatorname{M.D}(\bar{x})=\frac{f_{i}\left|x_{i}-\bar{x}\right|}{\mathrm{N}}  \tag{5}\\
& \operatorname{M.D}(\mathrm{M})=\frac{f_{i}\left|x_{i}-\mathrm{M}\right|}{\mathrm{N}} \tag{6}
\end{align*}
$$

where $x_{i}$ are the midpoints of the classes, $\bar{x}$ and M are, respectively, the mean and median of the distribution.
(c) Variance : Let $x_{1}, x_{2}, \ldots, x_{n}$ be $n$ observations with $\bar{x}$ as the mean. The variance, denoted by $\sigma^{2}$, is given by

$$
\begin{equation*}
\sigma^{2}=\frac{1}{n} \quad\left(x_{i}-\bar{x}\right)^{2} \tag{7}
\end{equation*}
$$

(d) Standard Deviation: If $\sigma^{2}$ is the variance, then $\sigma$, is called the standard deviation, is given by

$$
\begin{equation*}
\sigma=\sqrt{\frac{1}{n} \quad\left(x_{i}-\bar{x}\right)^{2}} \tag{8}
\end{equation*}
$$

(e) Standard deviation for a discrete frequency distribution is given by

$$
\begin{equation*}
\sigma=\sqrt{\frac{1}{\mathrm{~N}} \quad f_{i}\left(x_{i}-\bar{x}\right)^{2}} \tag{9}
\end{equation*}
$$

where $f_{i}^{\prime} \mathrm{s}$ are the frequencies of $x_{i}$ 's and $\mathrm{N}={ }_{i=1}^{n} f_{i}$.
(f) Standard deviation of a continuous frequency distribution (grouped data) is given by

$$
\begin{equation*}
\sigma=\sqrt{\frac{1}{\mathrm{~N}} \quad f_{i}\left(x_{i}-\bar{x}\right)^{2}} \tag{10}
\end{equation*}
$$

where $x_{i}$ are the midpoints of the classes and $f_{i}$ their respective frequencies. Formula (10) is same as

$$
\begin{equation*}
\sigma=\frac{1}{\mathrm{~N}} \sqrt{\mathrm{~N} \quad f_{i} x_{i}^{2}-\left(f_{i} x_{i}\right)^{2}} \tag{11}
\end{equation*}
$$

(g) Another formula for standard deviation :

$$
\begin{equation*}
\sigma_{x}=\frac{h}{\mathrm{~N}} \sqrt{\mathrm{~N} \quad f_{i} y_{i}^{2}-\left(f_{i} y_{i}\right)^{2}} \tag{12}
\end{equation*}
$$

where $h$ is the width of class intervals and $y_{i}=\frac{x_{i}-\mathrm{A}}{h}$ and A is the assumed mean.
15.1.2 Coefficient of variation It is sometimes useful to describe variability by expressing the standard deviation as a proportion of mean, usually a percentage. The formula for it as a percentage is

$$
\text { Coefficient of variation }=\frac{\text { Standard deviation }}{\text { Mean }} \times 100
$$

### 15.2 Solved Examples

## Short Answer Type

Example 1 Find the mean deviation about the mean of the following data:

| Size $(\boldsymbol{x}):$ | 1 | 3 | 5 | 7 | 9 | 11 | 13 | 15 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency $(\boldsymbol{f}):$ | 3 | 3 | 4 | 14 | 7 | 4 | 3 | 4 |

Solution Mean $=\bar{x}=\frac{f_{i} x_{i}}{f_{i}}=\frac{3+9+20+98+63+44+39+60}{42}=\frac{336}{42}=8$
M.D. $(\bar{x})=\frac{f_{i}\left|x_{i}-\bar{x}\right|}{f_{i}}=\frac{3(7)+3(5)+4(3)+14(1)+7(1)+4(3)+3(5)+4(7)}{42}$
$=\frac{21+15+12+14+7+12+15+28}{42}=\frac{62}{21}=2.95$
Example 2 Find the variance and standard deviation for the following data:
$57,64,43,67,49,59,44,47,61,59$
Solution Mean $(\bar{x})=\frac{57+64+43+67+49+59+61+59+44+47}{10}=\frac{550}{10}=55$

$$
\begin{aligned}
& \text { Variance }\left(\sigma^{2}\right)=\frac{\left(x_{i}-\bar{x}\right)^{2}}{n} \\
& =\frac{2^{2}+9^{2}+12^{2}+12^{2}+6^{2}+4^{2}+6^{2}+4^{2}+11^{2}+8^{2}}{10} \\
& = \\
& \frac{662}{10}=66.2
\end{aligned}
$$

Standard deviation $(\sigma)=\sqrt{\sigma^{2}}=\sqrt{66.2}=8.13$
Example 3 Show that the two formulae for the standard deviation of ungrouped data.

$$
\sigma=\sqrt{\frac{\left(x_{i}-\bar{x}\right)^{2}}{n}} \quad \text { and } \sigma^{\prime}=\sqrt{\frac{x_{i}^{2}}{n}-\bar{x}^{2}}
$$

are equivalent.
Solution We have

$$
\begin{aligned}
\left(x_{i}-\bar{x}\right)^{2} & =\left(x_{i}^{2}-2 \bar{x} x_{i}+\bar{x}^{2}\right) \\
& =x_{i}^{2}+-2 \bar{x} x_{i}+\bar{x}^{2} \\
& =x_{i}^{2}-2 \bar{x} x_{i}+(\bar{x})^{2} 1 \\
& =x_{i}^{2}-2 \bar{x}(n \bar{x})+n \bar{x}^{2} \\
& =x_{i}^{2}-n \bar{x}^{2}
\end{aligned}
$$

Dividing both sides by $n$ and taking their square root, we get $\sigma=\sigma^{\prime}$.
Example 4 Calculate variance of the following data :

| Class interval | Frequency |
| :---: | :---: |
| $4-8$ | 3 |
| $8-12$ | 6 |
| $12-16$ | 4 |
| $16-20$ | 7 |

$\operatorname{Mean}(\bar{x})=\frac{f_{i} x_{i}}{f_{i}}=\frac{3 \times 6+6 \times 10+4 \times 14+7 \times 18}{20}=13$

Solution Variance $\left(\sigma^{2}\right)=\frac{f_{i}\left(x_{i}-\bar{x}\right)^{2}}{f_{i}}=\frac{3(-7)^{2}+6(-3)^{2}+4(1)^{2}+7(5)^{2}}{20}$

$$
=\frac{147+54+4+175}{20}=19
$$

Long Answer Type
Example 5 Calculate mean, variation and standard deviation of the following frequency distribution:

| Classes | Frequency |
| :---: | :---: |
| $1-10$ | 11 |
| $10-20$ | 29 |
| $20-30$ | 18 |
| $30-40$ | 4 |
| $40-50$ | 5 |
| $50-60$ | 3 |

Solution Let A, the assumed mean, be 25.5. Here $h=10$

| Classes | $\boldsymbol{x}_{\boldsymbol{i}}$ | $\boldsymbol{y}_{\boldsymbol{i}}=\frac{\boldsymbol{x}_{\boldsymbol{i}}-\mathbf{2 5 . 5}}{\mathbf{1 0}}$ | $\boldsymbol{f}_{\boldsymbol{i}}$ | $\boldsymbol{f}_{\boldsymbol{i}} \boldsymbol{y}_{\boldsymbol{i}}$ | $\boldsymbol{f}_{\boldsymbol{i}} \boldsymbol{y}_{\boldsymbol{i}}^{\mathbf{2}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $1-10$ | 5.5 | -2 | 11 | -22 | 44 |
| $10-20$ | 15.5 | -1 | 29 | -29 | 29 |
| $20-30$ | 25.5 | 0 | 18 | 0 | 0 |
| $30-40$ | 35.5 | 1 | 4 | 4 | 4 |
| $40-50$ | 45.5 | 2 | 5 | 10 | 20 |
| $50-60$ | 55.5 | 3 | 3 | 9 | 27 |

$$
x^{\prime}=\frac{f_{i} y_{i}}{f_{i}}=\frac{-28}{70}=-0.4
$$

Mean $=\bar{x}=25.5+(-10)(0.4)=21.5$

Variance

$$
\left(\sigma^{2}\right)=\frac{h}{\mathrm{~N}}{\sqrt{\mathrm{~N} \quad f_{i} y_{i}^{2}-\left(f_{i} y_{i}\right)^{2}}}^{2}
$$

$$
=\frac{10 \times 10}{70 \times 70}\left[70(124)-(-28)^{2}\right]
$$

$$
=\frac{70(124)}{7 \times 7}-\frac{28 \times 28}{7 \times 7}=\frac{1240}{7}-16=161
$$

S.D. $(\sigma)=\sqrt{161}=12.7$

Example 6 Life of bulbs produced by two factories A and B are given below:

| Length of life <br> (in hours) | Factory A <br> (Number of bulbs) | Factory B <br> (Number of bulbs) |
| :---: | :---: | :---: |
| $550-650$ | 10 | 8 |
| $650-750$ | 22 | 60 |
| $750-850$ | 52 | 24 |
| $850-950$ | 20 | 16 |
| $950-1050$ | 16 | 12 |

The bulbs of which factory are more consistent from the point of view of length of life?
Solution Here $h=100$, let A (assumed mean) $=800$.


## For factory $\mathbf{A}$

$$
\begin{aligned}
\text { Mean }(\bar{x}) & =800+\frac{10}{120} \times 100=816.67 \text { hours } \\
\text { S.D. } & =\frac{100}{120} \sqrt{120(146)-100}=109.98
\end{aligned}
$$

Therefore, Coefficient of variation (C.V.) $=\frac{\text { S.D. }}{\bar{x}} \times 100=\frac{109.98}{816.67} \times 100=13.47$

## For factory B

$$
\begin{aligned}
& \text { Mean }=800+\frac{-36}{120} \quad 100=770 \\
& \text { S.D. }=\frac{100}{120} \sqrt{120(156)-(-36)^{2}}=110
\end{aligned}
$$

Therefore, Coefficient of variation $=\frac{\text { S.D. }}{\text { Mean }} \times 100=\frac{110}{770} \times 100=14.29$
Since C.V. of factory B $>$ C.V. of factory A $\Rightarrow$ Factory B has more variability which means bulbs of factory A are more consistent.

## Objective Type Questions

Choose the correct answer out of the four options given against each of the Examples 7 to 9 (M.C.Q.).

Example 7 The mean deviation of the data 2, 9, 9, 3, 6, 9, 4 from the mean is
(A) 2.23
(B) 2.57
(C) 3.23
(D) 3.57

Solution (B) is the correct answer

$$
\text { M.D. }(\bar{x})=\frac{\left|x_{i}-\bar{x}\right|}{n}=\frac{4+3+3+3+0+3+2}{7}=2.57
$$

Example 8 Variance of the data $2,4,5,6,8,17$ is 23.33 . Then variance of $4,8,10,12$, 16,34 will be
(A) 23.23
(B) 25.33
(C) 46.66
(D) 48.66

Solution (C) is the correct answer. When each observation is multiplied by 2, then variance is also multiplied by 2 .

Example 9 A set of $n$ values $x_{1}, x_{2}, \ldots, x_{n}$ has standard deviation 6. The standard deviation of $n$ values $x_{1}+k, x_{2}+k, \ldots, x_{n}+k$ will be
(A) $\sigma$
(B) $\sigma+k$
(C) $\sigma-k$
(D) $k \sigma$

Solution (A) is correct answer. If each observation is increased by a constant $k$, then standard deviation is unchanged.

### 15.3 EXERCISE

## Short Answer Type

1. Find the mean deviation about the mean of the distribution:

| Size | 20 | 21 | 22 | 23 | 24 |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Frequency | 6 | 4 | 5 | 1 | 4 |

2. Find the mean deviation about the median of the following distribution:

| Marks obtained | 10 | 11 | 12 | 14 | 15 |
| :--- | ---: | ---: | ---: | ---: | ---: |
| No. of students | 2 | 3 | 8 | 3 | 4 |

3. Calculate the mean deviation about the mean of the set of first $n$ natural numbers when $n$ is an odd number.
4. Calculate the mean deviation about the mean of the set of first $n$ natural numbers when $n$ is an even number.
5. Find the standard deviation of the first $n$ natural numbers.
6. The mean and standard deviation of some data for the time taken to complete a test are calculated with the following results:
Number of observations $=25$, mean $=18.2$ seconds, standard deviation $=3.25$ seconds.
Further, another set of 15 observations $x_{1}, x_{2}, \ldots, x_{15}$, also in seconds, is now available and we have $x_{i=1}^{15} x_{i}=279$ and $x_{i=1}^{15}=5524$. Calculate the standard derivation based on all 40 observations.
7. The mean and standard deviation of a set of $n_{1}$ observations are $\bar{x}_{1}$ and $s_{1}$, respectively while the mean and standard deviation of another set of $n_{2}$ observations are $\bar{x}_{2}$ and $s_{2}$, respectively. Show that the standard deviation of the combined set of $\left(n_{1}+n_{2}\right)$ observations is given by
S.D. $=\sqrt{\frac{n_{1}\left(s_{1}\right)^{2}+n_{2}\left(s_{2}\right)^{2}}{n_{1}+n_{2}}+\frac{n_{1} n_{2}\left(\bar{x}_{1}-\bar{x}_{2}\right)^{2}}{\left(n_{1}+n_{2}\right)^{2}}}$
8. Two sets each of 20 observations, have the same standard derivation 5. The first set has a mean 17 and the second a mean 22 . Determine the standard deviation of the set obtained by combining the given two sets.
9. The frequency distribution:

| $\boldsymbol{x}$ | A | 2 A | 3 A | 4 A | 5 A | 6 A |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{f}$ | 2 | 1 | 1 | 1 | 1 | 1 |

where $A$ is a positive integer, has a variance of 160 . Determine the value of $A$.
10. For the frequency distribution:

| $\boldsymbol{x}$ | 2 | 3 | 4 | 5 | 6 | 7 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{f}$ | 4 | 9 | 16 | 14 | 11 | 6 |

Find the standard distribution.
11. There are 60 students in a class. The following is the frequency distribution of the marks obtained by the students in a test:

| Marks | 0 | 1 | 2 | 3 | 4 | 5 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | $x-2$ | $x$ | $x^{2}$ | $(x+1)^{2}$ | $2 x$ | $x+1$ |

where $x$ is a positive integer. Determine the mean and standard deviation of the marks.
12. The mean life of a sample of 60 bulbs was 650 hours and the standard deviation was 8 hours. A second sample of 80 bulbs has a mean life of 660 hours and standard deviation 7 hours. Find the overall standard deviation.
13. Mean and standard deviation of 100 items are 50 and 4 , respectively. Find the sum of all the item and the sum of the squares of the items.
14. If for a distribution $(x-5)=3, \quad(x-5)^{2}=43$ and the total number of item is 18 , find the mean and standard deviation.
15. Find the mean and variance of the frequency distribution given below:

| $\boldsymbol{x}$ | $1 \leq x<3$ | $3 \leq x<5$ | $5 \leq x<7$ | $7 \leq x<10$ |
| :---: | :---: | :---: | ---: | :---: | :---: |
| $\boldsymbol{f}$ | 6 | 4 | 5 | 1 |

## Long Answer Type

16. Calculate the mean deviation about the mean for the following frequency distribution:

| Class interval | $0-4$ | $4-8$ | $8-12$ | $12-16$ | $16-20$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Frequency | 4 | 6 | 8 | 5 | 2 |

17. Calculate the mean deviation from the median of the following data:

| Class interval | $0-6$ | $6-12$ | $12-18$ | $18-24$ | $24-30$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Frequency | 4 | 5 | 3 | 6 | 2 |

18. Determine the mean and standard deviation for the following distribution:

| Marks | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | :---: |
| Frequency | 1 | 6 | 6 | 8 | 8 | 2 | 2 | 3 | 0 | 2 | 1 | 0 | 0 | 0 | 1 |

19. The weights of coffee in 70 jars is shown in the following table:

| Weight <br> (in grams) | Frequency |
| :---: | :---: |
| $200-201$ | 13 |
| $201-202$ | 27 |
| $202-203$ | 18 |
| $203-204$ | 10 |
| $204-205$ | 1 |
| $205-206$ | 1 |

Determine variance and standard deviation of the above distribution.
20. Determine mean and standard deviation of first $n$ terms of an A.P. whose first term is $a$ and common difference is $d$.
21. Following are the marks obtained, out of 100 , by two students Ravi and Hashina in 10 tests.

| Ravi | 25 | 50 | 45 | 30 | 70 | 42 | 36 | 48 | 35 | 60 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Hashina | 10 | 70 | 50 | 20 | 95 | 55 | 42 | 60 | 48 | 80 |

Who is more intelligent and who is more consistent?
22. Mean and standard deviation of 100 observations were found to be 40 and 10 , respectively. If at the time of calculation two observations were wrongly taken as 30 and 70 in place of 3 and 27 respectively, find the correct standard deviation.
23. While calculating the mean and variance of 10 readings, a student wrongly used the reading 52 for the correct reading 25 . He obtained the mean and variance as 45 and 16 respectively. Find the correct mean and the variance.

## Objective Type Questions

Choose the correct answer out of the given four options in each of the Exercises 24 to 39 (M.C.Q.).
24. The mean deviation of the data $3,10,10,4,7,10,5$ from the mean is
(A) 2
(B) 2.57
(C) 3
(D) 3.75
25. Mean deviation for $n$ observations $x_{1}, x_{2}, \ldots, x_{n}$ from their mean $\bar{x}$ is given by
(A) ${ }_{i=1}^{n}\left(x_{i}-\bar{x}\right)$
(B) $\frac{1}{n}{ }_{i=1}^{n}\left|x_{i}-\bar{x}\right|$
(C) ${ }_{i=1}^{n}\left(x_{i}-\bar{x}\right)^{2}$
(D) $\frac{1}{n}_{i=1}^{n}\left(x_{i}-\bar{x}\right)^{2}$
26. When tested, the lives (in hours) of 5 bulbs were noted as follows:

1357, 1090, 1666, 1494, 1623
The mean deviations (in hours) from their mean is
(A) 178
(B) 179
(C) 220
(D) 356
27. Following are the marks obtained by 9 students in a mathematics test: $50,69,20,33,53,39,40,65,59$
The mean deviation from the median is:
(A) 9
(B) 10.5
(C) 12.67
(D) 14.76
28. The standard deviation of the data $6,5,9,13,12,8,10$ is
(A) $\sqrt{\frac{52}{7}}$
(B) $\frac{52}{7}$
(C) $\sqrt{6}$
(D) 6
29. Let $x_{1}, x_{2}, \ldots, x_{n}$ be $n$ observations and $\bar{x}$ be their arithmetic mean. The formula for the standard deviation is given by
(A) $\quad\left(x_{i}-\bar{x}\right)^{2}$
(B) $\frac{\left(x_{i}-\bar{x}\right)^{2}}{n}$
(C) $\sqrt{\frac{\left(x_{i}-\bar{x}\right)^{2}}{n}}$
(D) $\sqrt{\frac{x_{i}^{2}}{n}+\bar{x}^{2}}$
30. The mean of 100 observations is 50 and their standard deviation is 5 . The sum of all squares of all the observations is
(A) 50000
(B) 250000
(C) 252500
(D) 255000
31. Let $a, b, c, d, e$ be the observations with mean $m$ and standard deviation $s$. The standard deviation of the observations $a+k, b+k, c+k, d+k, e+k$ is
(A) $s$
(B) $k s$
(C) $s+k$
(D) $\frac{s}{k}$
32. Let $x_{1}, x_{2}, x_{3}, x_{4}, x_{5}$ be the observations with mean $m$ and standard deviation $s$. The standard deviation of the observations $k x_{1}, k x_{2}, k x_{3}, k x_{4}, k x_{5}$ is
(A) $k+s$
(B) $\frac{s}{k}$
(C) $k s$
(D) $s$
33. Let $x_{1}, x_{2}, \ldots x_{n}$ be $n$ observations. Let $w_{i}=l x_{i}+k$ for $i=1,2, \ldots n$, where $l$ and $k$ are constants. If the mean of $x_{i}{ }^{\prime} s$ is 48 and their standard deviation is 12 , the mean of $w_{i}^{\prime} s$ is 55 and standard deviation of $w_{i} ' s$ is 15 , the values of $l$ and $k$ should be
(A) $l=1.25, k=-5$
(B) $l=-1.25, k=5$
(C) $l=2.5, k=-5$
(D) $l=2.5, k=5$
34. Standard deviations for first 10 natural numbers is
(A) 5.5
(B) 3.87
(C) 2.97
(D) 2.87
35. Consider the numbers $1,2,3,4,5,6,7,8,9,10$. If 1 is added to each number, the variance of the numbers so obtained is
(A) 6.5
(B) 2.87
(C) 3.87
(D) 8.25
36. Consider the first 10 positive integers. If we multiply each number by -1 and then add 1 to each number, the variance of the numbers so obtained is
(A) 8.25
(B) 6.5
(C) 3.87
(D) 2.87
37. The following information relates to a sample of size 60: $x^{2}=18000$,

$$
x=960
$$

The variance is
(A) 6.63
(B) 16
(C) 22
(D) 44
38. Coefficient of variation of two distributions are 50 and 60 , and their arithmetic means are 30 and 25 respectively. Difference of their standard deviation is
(A) 0
(B) 1
(C) 1.5
(D) 2.5
39. The standard deviation of some temperature data in ${ }^{\circ} \mathrm{C}$ is 5 . If the data were converted into ${ }^{\circ} \mathrm{F}$, the variance would be
(A) 81
(B) 57
(C) 36
(D) 25

Fill in the blanks in Exercises from 40 to 46.
40. Coefficient of variation $=\frac{\ldots}{\text { Mean }} \times 100$
41. If $\bar{x}$ is the mean of $n$ values of $x$, then $\quad\left(x_{i}-\bar{x}\right)$ is always equal to $\qquad$ .

If $a$ has any value other than $\bar{x}$, then ${ }_{i=1}^{n}\left(x_{i}-\bar{x}\right)^{2}$ is ______ than

$$
\left(x_{i}-a\right)^{2}
$$

42. If the variance of a data is 121 , then the standard deviation of the data is $\qquad$ .
43. The standard deviation of a data is $\qquad$ of any change in orgin, but is
$\qquad$ on the change of scale.
44. The sum of the squares of the deviations of the values of the variable is $\qquad$ when taken about their arithmetic mean.
45. The mean deviation of the data is $\qquad$ when measured from the median.
46. The standard deviation is $\qquad$ to the mean deviation taken from the arithmetic mean.
$\qquad$
